

A new approach for cell formation and scheduling with assembly operations and product structure

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ABSTRACT

In this paper, a new formulation model for cellular manufacturing system (CMS) design problem is proposed. The proposed model of this paper considers assembly operations and product structure so that it includes the scheduling problem with the formation of manufacturing cells, simultaneously. Since the proposed model is nonlinear, a linearization method is applied to gain optimal solution when the model is solved using direct implementation of mixed integer programming. A new genetic algorithm (GA) is also proposed to solve the resulted model for large-scale problems. We examine the performance of the proposed method using the direct implementation and the proposed GA method. The results indicate that the proposed GA approach could provide efficient assembly and product structure for real-world size problems.

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1. Introduction

Cellular manufacturing system (CMS) is one of the most important tools on improving the flexibility of any production planning (McAuley, 1972). CMS is considered to be one of the most interesting applications of group technology (GT) and it can significantly influence the batch production and increases the overall performance of a production plan. CMS is a successful alternative in response to today's manufacturing requirements and it can reduce the unnecessary transportation among different cells. On the other hand, a good assembly plans can reduce the makespan of the final product which leads to lower total production cost. During the past two decades, there have been tremendous works dedicated on developing meta-heuristic approaches for CMS to provide efficient solutions (Gosh, et al., 2010). There are different types of mathematical models to address various aspects of CMS problem and one of the interesting ones is to study on assembly operations and product structure. The CMS problem can be categorized into three following groups.

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The first CMS group is dedicated to the assignment of parts to machines. One of the basic applications of CMS design is to propose a plan to allocate different parts to various groups of machines. Schaller et al. (2000) considered scheduling part families and jobs within each part family in a flowline manufacturing cell where the setup times for each family were sequence dependent and it was desired to minimize the makespan. Park and Kim (2000) focused on a production scheduling problem in a tree-structured assembly system and considered due dates as constraints in the problem without considering tardiness. They suggested a branch-and-bound algorithm to solve the proposed mixed integer linear programming model and used a Lagrangian relaxation method in which a subgradient method was also employed to obtain lower bounds for the subproblems. Park and Mutingi (2001) presented a meta-heuristic based cell formation procedure where the problem was to simultaneously group machines and part families into cells. The cell formation problem (CFP) was modeled with three different objectives: minimization of inter-cellular movements due to exceptional parts, minimizing intra-cell work load imbalances, and combination of these two options. The GA was used to solve the problems and allowed to specify the number of cells required a priori and impose lower and upper bounds on cell size to make the GA scheme flexible to solve the CFPs. Franca et al. (2005) considered the makespan minimization while considering processing parts (jobs) in each family, simultaneously. This type of scheduling problem includes part families and jobs in which each part family in a flowshop manufacturing cell with sequence dependent family setups times was also considered. Boulif and Atif (2006) proposed a graph partitioning formulation of CFP which combines the branch-and-bound and GA methods. They considered some of the real-world circumstances including both practical input data (e.g. operation sequence and part demands) and realistic constraints (e.g. machine cohabitation and non-cohabitation). Also, cohabitation and non-cohabitation constraints were also considered to treat the special cases of machines. Hu and Yasuda (2006) considered cell formation problem with alternative processing routes where the number of manufacturing cells was unknown in advance. They also adopted grouping genetic algorithm (GGA) in which a new chromosome representation, a local optimization algorithm for crossover operator and special mutation operators were developed to solve their problem formulation. Wu et al. (2007) proposed a new approach to concurrently determine the cell formation (CF), group layout (GL) and group scheduling (GS) decisions in CMS design. A conceptual framework and mathematical model, which integrates these three decisions, were presented. Also, a hierarchical genetic algorithm was developed to solve the integrated cell design problem. The results from their study indicated that these three decisions (i.e. CF, GL and GS) must be considered simultaneously in order to obtain better results. Tavakkoli-Moghaddam et al. (2008) presented a group scheduling problem for manufacturing by considering inter-cell scheduling and the sequence of cells. They also considered the cell scheduling problem in the presence of bottleneck machines and exceptional elements incurring inter-cell movement costs in CM. They proposed genetic and memetic algorithms to solve the given problem and evaluated the performance of their proposed algorithms by generating numerous data, randomly.

The second group of CMS problems deals with converting from assembly lines to assembly cells. The assembly cells are usually formed by creating teams of workers where each team is responsible for a specific set of assembly tasks. The performance improvement from conversion of an assembly line to assembly cells and the factors which influence these improvements are different than the tradeoffs to be investigated when a functional layout is converted to cells. Sengupta and Jacobs (1998) stated that the cellular systems outperform an unpaced assembly line when teamwork is efficient and task time variances and setup times are high. In contrast, the assembly line outperforms the cells when task time variances and setup times are low and/or when teamwork in the cells causes an increase in assembly task time. In addition, Sengupta and Jacobs (2004) compared a conventional serial assembly line with two different configurations of assembly cells using the simulation models. They implemented their models on a real-world case study of television industry to understand the effects of the different factors in order to see which type of system works better. Johnson (2005) also emphasized that prior researches on various factors influencing performance improvement through

cell conversions primarily focused on the conversion from a functional to a cellular layout. He also used simulation model using some real-world data to measure the impact of each factor on the estimated performance improvement resulted by converting assembly lines to assembly cells.

The third group of CFM problems is the integration of part assembly and CMS design problem. Panchalavarapu and Chankong (2005) studied assembly aspects in the context of cell formation problem (CFP) and proposed a new idea of assembling the parts in the same cells where the production of the parts happen. They also proposed a mathematical model which uses a new similarity coefficient among part, machine and subassembly to determine the suitable assignments to manufacturing cells. Their model employed a part-subassembly incidence matrix derived from the product structure. Aryanezhad and Aliabadi (2010) developed a nonlinear model to integrate the assembly details and product structure to the CFP where both machining and assembly operations were considered together to minimize the intercellular movements.

In this paper, we present a new integrated method to consider both assembly operations and cell formation. The resulted problem formulation is nonlinear mixed integer optimization problem. The resulted problem is reformulated into a standard mixed integer programming where a traditional optimization toolbox could find the optimal solutions for small-scale instances. We also develop a GA method to provide solution procedure for real-world large-scale problems. This paper is organized as follows. The problem statement of the proposed method is given in section 2. Section 3 develops a new GA to solve the aforementioned model for large-size problems. The computational results by LINGO and proposed GA for different examples in literature are reported in Section 4. Finally, Section 5 summarizes the contribution of the research.

2. Problem description of and modeling

As we explained before the proposed model of this paper considers the assembly details to form the manufacturing cells and scheduling the operations, simultaneously. The assembly operations are required to be performed in a specific order for making the final products. This order is usually represented with product structure known as bill of material (BOM). This tree diagram can be composed in any number of levels in which a set of lower level components called child are transformed to a component of higher level called parent. In this paper, one final product with simple structure is considered in which the assembled components are divided into two types: *individual parts* or the parts which contain only the machining consecutive operations and their role is always child and *assembly items* which are the items such as final product and they are composed from a number of components and do not need any machining operations. Fig.1 shows an example of product structure for one finished product in which the subassemblies are indicated with SA_i and individual parts are placed in the lowest levels.

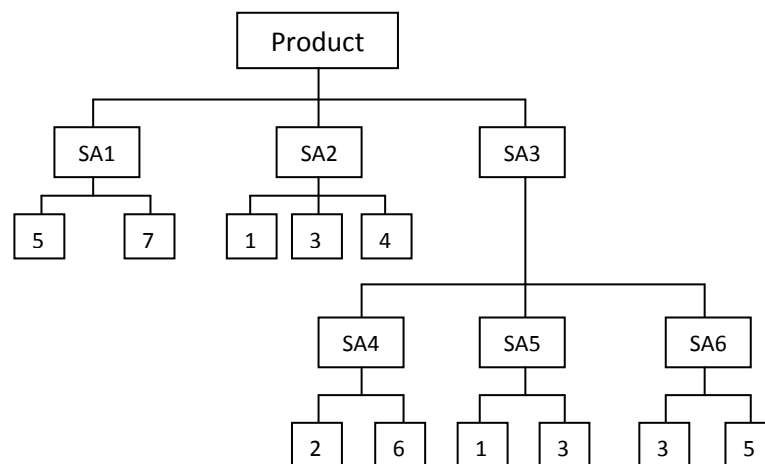


Fig.1. An example of product structure

The following assumptions are used for the proposed model of this paper.

- Production volume of each component depends on demand for final product and it is identified based on the production volume of higher level components.
- Each parent item could have any number from a type of its children.
- Both machining and assembly operations are just accomplished in one cell and each cell is limited by a lower bound and an upper bound.
- On the contrary to the traditional models, we assume that the number of cells is one of the unknown variables and it is not predefined.
- Intra-cell and inter-cell movement times of each component and duration times for setting up and performing machining operations are given. In addition, assembly times and setup times for assembly are also known.
- The setup times on each machine are specified based on the precedence of parts. This assumption obviates the common drawback in other studies in which the machine setup time is considered when different part families are substituted on a certain machine. However, part families are not predefined, because grouping parts into some families does not need to be considered as a stage of cell formation and also defining a decision variable for assigning the part family number to each part is not helpful. On the other hand, grouping different types of parts in one family and for any reason like similarities in processing does not mean that the parts have equal setup time. Therefore, we consider $ST_{pp'}^m$ as the required time for preparing the machine m for processing part p' after the previous processing task on part p by the same machine.

2.1. Indices

- p : Index indicating individual part types which contain only the machining operations ($p=1,2,\dots,P$);
- r : Index of alternative process routes (APR) for individual part type p ($r=1,2,\dots,R_p$);
- q : Index of operations on route r of individual part type p ($q=1,2,\dots,Q_{pr}$);
- m : Index of machine types ($m=1,2,\dots,M$);
- i : Index of assembly items which are composed from a number of components and do not have machining operations ($i=P+1,P+2,\dots,I$; $i=I$ is the finished product);
- $IDE_i \{j\}$: Immediate children set of parent I ; each j can be either individual part or assembly item
- l : Index of cells ($l=1, 2,\dots, C$);

2.2. Input parameters

- $v_p (v_i)$: Production volume of individual part type p (assembly item type i) in terms of cycle time.
- TA_p
(TA_i): Time of intra-cell movement for batch of individual part p (assembly item i)
- TE_p
(TE_i): Time of inter-cell movement for batch of individual part p (assembly item i)
- t_{prq} : Duration time for processing the q -th operation on route r of part type p per unit
- t_i : Assembly time of one unit of parent item type i
- $ST_{pp'}^m$: Setup time for processing part type p' on machine type m after processing part type p

ST_i : Setup time for assembling parent item type i

T_m : Time capacity of machine type m

LB : Minimum number of machines allowed in each cell

UB : Maximum number of machines allowed in each cell

L_∞ : Large positive number

$$a_{m_{pr}^q} = \begin{cases} 1, & \text{if } q\text{-th operation on route } r \text{ of part type } p \text{ is processed by machine type } m \\ 0, & \text{otherwise} \end{cases}$$

2.3. Decision variables

$$X_{ml} = \begin{cases} 1, & \text{if machine type } m \text{ is allocated to cell } l \\ 0, & \text{otherwise} \end{cases}$$

In the proposed model, m_{pr}^q sometimes is substituted to m in the X_{ml} to indicate the machine type m is assigned to q -th operation on route r of part type p . In fact, $X_{(m_{pr}^q)l}$ is equal to $a_{m_{pr}^q} \cdot X_{ml}$ and is used instead of the aforementioned multiplication.

$$Y_{pl} = \begin{cases} 1, & \text{if route } r \text{ is selected for part type } p \\ 0, & \text{otherwise} \end{cases}$$

$$Z_{il} = \begin{cases} 1, & \text{if item } i \text{ is assembled in cell } l \\ 0, & \text{otherwise} \end{cases}$$

$$C_l = \begin{cases} 1, & \text{if cell } l \text{ is formed} \\ 0, & \text{otherwise} \end{cases}$$

$$u_{pp'}^m = \begin{cases} 1, & \text{if part type } p \text{ is processed by machine } m \text{ before part type } p' \\ 0, & \text{otherwise} \end{cases}$$

$ST_{oo'}^m$: Start time of q -th operation on route r of part type p

S_i : Start time of assembly operation of parent item type i

2.4. Mathematical model

The following represents the mathematical formulation of the proposed model. The objective function in Eq. (1) minimizes the cycle time of producing the given volume of finished product in manufacturing system. For this purpose, Eq. (2) to Eq. (8) are considered to compute the start time of

finished product (S_j). Eq. (2) computes the time of movement between two consecutive operations for each part. Constraint (3) is to ensure that the starting time of machining operations performed on each part depends on their sequences.

$$\min CT = \{S_I + v_I t_I\} \quad (1)$$

subject to

$$t_{pr(q,q+1)} = \sum_{l=1}^C \left[Y_{pr} X_{(m_{pr}^q)_l} \left(TA_p X_{(m_{pr}^{q+1})_l} + TE_p (1 - X_{(m_{pr}^{q+1})_l}) \right) \right] \quad \forall p, r, q < Q_{pr} \quad (2)$$

$$S_{prq} + v_p t_{prq} + t_{pr(q,q+1)} \leq S_{pr(q+1)} + (1 - Y_{pr}) L_\infty \quad \forall p, r, q < Q_{pr} \quad (3)$$

$$S_{prq} + v_p t_{prq} + ST_{pp'}^m \leq S_{(prq)'} + L_\infty \left[(1 - u_{pp'}^m) + (1 - a_{m_{pr}^q} Y_{pr}) + (1 - a_{(m_{pr}^q)'} Y_{(pr)'}) \right] \quad \forall m, prq, (prq)' \quad (4)$$

$$t_{jrQ,i} = \sum_{l=1}^C \left[Y_{jr} X_{(m_{jr}^Q)_l} \left(TA_j Z_{il} + TE_j (1 - Z_{il}) \right) \right] \quad \forall i, j \in IDE_i, r_j \quad (5)$$

$$S_{jrQ} + v_j t_{jrQ} + t_{jrQ,i} + ST_i \leq S_i + (1 - Y_{jr}) L_\infty \quad \forall i, j \in IDE_i, r_j \quad (6)$$

$$t_{(j,i)} = \sum_{l=1}^C \left[Z_{jl} \left(TA_j Z_{il} + TE_j (1 - Z_{il}) \right) \right] \quad \forall i, j \in IDE_i \quad (7)$$

$$S_j + v_j t_j + t_{(j,i)} + ST_i \leq S_i \quad \forall i, j \in IDE_i \quad (8)$$

$$\sum_{r=1}^{R_p} Y_{pr} = 1 \quad \forall p \quad (9)$$

$$\sum_{l=1}^C Z_{il} = 1 \quad \forall i \quad (10)$$

$$\sum_{l=1}^C X_{ml} = 1 \quad \forall m \quad (11)$$

$$2C_l \geq Z_{il} + X_{ml} \quad \forall i, m, l \quad (12)$$

$$LB \cdot C_l \leq \sum_{m=1}^C X_{ml} \leq UB \cdot C_l \quad \forall l \quad (13)$$

$$\sum_{p=1}^P \sum_{r=1}^{R_p} \sum_{q=1}^{Q_{pr}} \left[v_p Y_{pr} t_{prq} a_{m_{pr}^q} \right] \leq T_m \quad \forall m \quad (14)$$

$$Y_{pr}, X_{ml}, Z_{il}, C_l = \{0, 1\} \quad \forall p, r, q, i, m, l \quad (15)$$

$$S_i, S_{prq} \geq 0 \quad \forall p, r, q, i$$

$$u_{pp'}^m = \{0, 1\} \quad \forall m, prq, (prq)'$$

Constraint (4) considers precedence of parts which need to be processed on a given machine so that only one operation can be done, simultaneously. Eq. (5) and Eq. (7) calculate the transfer time of child item j to place of assembling parent item i depending on whether child item has the machining operation or it is assembly item, respectively. Eq. (6) and Eq. (8) adjust the requirement conditions of assembly start times based on product structure, correspondingly. Constraint (9) indicates that only one route for each part type which contains machining operation must be selected. Constraints (10) and (11) indicate that each assembly operation and machine type respectively are assigned to one cell. Constraint (12) ensures that a cell is formed if assembly or machining operation is assigned to it.

Constraint (13) limits the minimum and the maximum number of machines in each cell. Time capacity allowed of each machine is limited by constraint (14). Finally, Eq. (15) specifies situation of decision variables.

2.5. Linearization

As we can observe, there are some nonlinear terms in the structure of problem formulation such as the existing term $Y_{pr} X_{(m_{pr}^q)l} X_{(m_{pr}^{q+1})l}$ in equation (8). For each nonlinear term, a new auxiliary variable is defined as follows,

$$U_{(m_{pr}^q)l} = Y_{pr} X_{(m_{pr}^q)l} X_{(m_{pr}^{q+1})l} \quad \forall p, r, q < Q_{pr}, l \tag{16}$$

$$W_{(m_{pr}^q)l} = Y_{pr} X_{(m_{pr}^q)l} (1 - X_{(m_{pr}^{q+1})l}) \quad \forall p, r, q < Q_{pr}, l \tag{17}$$

$$G_{ijl} = Z_{jl} Z_{il} \quad \forall i, j \in IDE_i, l \tag{18}$$

$$H_{ijl} = Z_{jl} (1 - Z_{il}) \quad \forall i, j \in IDE_i, l \tag{19}$$

$$QAU_{ijrl} = Y_{jr} X_{(m_{jr}^q)l} Z_{il} \quad \forall i, j \in IDE_i, r, l \tag{20}$$

$$QAW_{ijrl} = Y_{jr} X_{(m_{jr}^q)l} (1 - Z_{il}) \quad \forall i, j \in IDE_i, r, l \tag{21}$$

Based on Eq. (16) and Eq. (17), $U_{(m_{pr}^q)l}$ is equal to zero when two consecutive operations q and $q+1$ of part p are performed in two distinct cells; but in this situation, $W_{(m_{pr}^q)l}$ is equal to 1. For the parent/child relationships where both components are the assembly items, if the cell assigned to assembly operation of parent item (related to Z_{il}) is different from the corresponding cell of child (related to Z_{jl}), G_{ijk} is equal to 0 and H_{ijk} is equal to 1. Similarly, QAW_{ijrl} is equal to 1 and QAU_{ijrl} is equal to 0 when for a pair of parent and child where child has machining operation, the assembly operation of the parent and the last machining operation of child is not performed in the same cell. Thus, in terms of the right hand side value of each new variable, two corresponding linearization constraints are also added which are as follows,

- ◆ Constraints of new decision variable $U_{(m_{pr}^q)l}$

$$U_{(m_{pr}^q)l} \geq Y_{pr} X_{(m_{pr}^q)l} X_{(m_{pr}^{q+1})l} - 2 \quad \forall p, r, q < Q_{pr}, l \tag{22}$$

$$3 U_{(m_{pr}^q)l} \leq Y_{pr} X_{(m_{pr}^q)l} X_{(m_{pr}^{q+1})l} \quad \forall p, r, q < Q_{pr}, l \tag{23}$$

- ◆ Constraints of new decision variable $W_{(m_{pr}^q)l}$

$$W_{(m_{pr}^q)l} \geq Y_{pr} X_{(m_{pr}^q)l} (1 - X_{(m_{pr}^{q+1})l}) - 2 \quad \forall p, r, q < Q_{pr}, l \tag{24}$$

$$3 W_{(m_{pr}^q)l} \leq Y_{pr} X_{(m_{pr}^q)l} (1 - X_{(m_{pr}^{q+1})l}) \quad \forall p, r, q < Q_{pr}, l \tag{25}$$

- ◆ Constraints of new decision variable G_{ijl}

$$G_{ijl} \geq Z_{jl} + Z_{il} - 1 \quad \forall i, j \in IDE_i, l \tag{26}$$

$$2 G_{ijl} \leq Z_{jl} + Z_{il} \quad \forall i, j \in IDE_i, l \tag{27}$$

- ◆ Constraints of new decision variable H_{ijl}

$$H_{ijl} \geq Z_{jl} + (1 - Z_{il}) - 1 \quad \forall i, j \in IDE_i, l \tag{28}$$

$$2 H_{ijl} \leq Z_{jl} + (1 - Z_{il}) \quad \forall i, j \in IDE_i, l \quad (29)$$

◆ Constraints of new decision variable QAU_{ijrl}

$$QAU_{ijrl} \geq Y_{jr} + X_{(m_r^o)l} + Z_{il} - 2 \quad \forall i, j \in IDE_i, r, l \quad (30)$$

$$3 QAU_{ijrl} \geq Y_{jr} + X_{(m_r^o)l} + Z_{il} \quad \forall i, j \in IDE_i, r, l \quad (31)$$

◆ Constraints of new decision variable QAW_{ijrl}

$$QAW_{ijrl} \geq Y_{jr} + X_{(m_r^o)l} + (1 - Z_{il}) - 2 \quad \forall i, j \in IDE_i, r, l \quad (32)$$

$$3 QAW_{ijrl} \geq Y_{jr} + X_{(m_r^o)l} + (1 - Z_{il}) \quad \forall i, j \in IDE_i, r, l \quad (33)$$

3. Proposed genetic algorithm

In this section, we present a GA to solve the proposed model for some large-size problems. GA, popularized by Holland (1975), has been employed effectively to get good quality solutions for a wide range of optimization problems such as scheduling problems (e.g. Reeves, 1995; Ruiz et al. 2006). GA begins with an initial set of solutions, namely, population of chromosomes, which are promoted during consecutive iterations by genetic operators (i.e. selection, crossover and mutation). In addition, a fitness value is assigned to each chromosome in accordance with the objective function. The new offspring are produced regarding to current population for each iteration.

3.1. Chromosomes representation

In the proposed algorithm, the decision variables are represented as follows.

1. Cells dedicated to each machine (CDM): A chromosome is considered which has as many genes as the number of the machines and array genes contain the cell number assigned to each machine. For example, suppose we have 5 machines and 3 cells, the solution for assigning machines number 2 and 4 to cell number 1, machines number 1 and 3 to cell number 2, and machine number 5 to cell number 3 is represented in an array of the following form:

2	1	2	1	3
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2. Cells assigned to assembly operations (CAO): To show this, assume as many genes as existing parts in the system. If part has assembly operation, corresponding gene is assigned the cell number where the assembly is performed in, or else corresponding gene is assigned 0.

0	2	0	0	2	1
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3. Processing routes of parts (PRP): For each part which has machining operation, the processing route number is stored in a distinct gene otherwise it is assigned 0. For example, if there are 7 parts, we can put them in 7 genes from left to right, as shown below. Each gene number shows the number of selected route for corresponding part. So, it is clear that part 5 does not have machining operation.

1	3	2	1	0	2	1
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4. Order of parts for entrancing to objective functions (OPE): This chromosome shows priority of parts concerning together for entrancing to time objective function. To show this parameter, assume as many genes as existing parts and sort parts according to their priorities. For instance, if we have 7 parts, the following shows the processing priority of parts.

4	2	3	1	5	7	6
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3.2. Parents' selection mechanism

In this paper, one of the parents is selected based on *roulette wheel* method and the other one is selected, uniformly. The selection mechanism in roulette wheel is that the parents with more value of fitness are more appropriate to be selected. In other words, chromosomes with shorter waiting time are chosen for crossover. Thus, chromosomes are sorted in descending order so that the probability of selection for each chromosome is calculated in the following way.

$$P_k = \frac{2k}{M(M+1)} \quad k = 1, \dots, \text{popsize} \quad (34)$$

The cumulative probability of chromosomes to point s is calculated using the below equation.

$$q_s = \sum_{j=1}^s p_j \quad 2 \leq s \leq \text{popsize} \quad (35)$$

Then, for each chromosome in population, a random number r between 0 and 1 is generated. If $r < q_1$, the first chromosome is selected, otherwise the s -th chromosome is selected such that $q_{s-1} < r \leq q_s$.

3.3. Crossover and Mutation Operators

The crossover operators used in the proposed genetic algorithm are single-point and the mutation approach is displacement in which a random point is selected randomly and inserted in another place. These operators are considered for all iterations of the algorithm so that the infeasible solutions are not generated.

3.4. Proposed algorithm

The following shows the steps of the proposed algorithm.

Step 1: Generate initial population

Step 2: Sort population in decreasing order of fitness function

Step 3: if termination criteria satisfied {END} Else {Go to 4;}

Step 4: Let $X = \text{RANDOM}[0,1]$; If $X < R_c$ {Go to 5;} Else {Go to 6;}

Step 5: Select two chromosomes for CDM, CAO and PRP

Step 6: Let $X = \text{Random}[0,1]$; if $X < R_m$ {Go to 7;} Else {Go to 8;}

Step 7: Mute crossed chromosome for CDM, CAO and PRP

Step 8: if Generated solution is better than a solution among population replace it among population;

Step 9: Set $i=0$;

Step 10: if $i < \text{Rep}$ {Go to 11} Else {Go to 17;}

Step 11: Let $X = \text{RANDOM}[0,1]$; If $X < R_c$ {Go to 12;} Else {Go to 13;}

Step 12: Select two chromosomes for OPE

Step 13: Let $X = \text{Random}[0,1]$; if $X < R_m$ {Go to 14;} Else {Go to 15;}

Step 14: Mute crossed chromosome for OPE

Step 15: if Generated solution is better than a solution among population replace it among population; Else {Go to 9;}

Step 16: Set $i=i+1$; Go to 10;

Step 17: Go to 2

4. Computational results

4.1 Calibration of algorithm parameters; Taguchi method

We use an experimental design of Taguchi to calibrate the parameters of our proposed algorithm. In this method, controllable factors are placed in inner orthogonal array, noise factors in the outer orthogonal array. This method changes the quality attributes into signal to noise ratio in order to locate the optimized levels of the useful factors in the experiments. In this design of experiment method, signal to noise ratio minimizes the variance and mean quality attributes to make them closer to the expected values. The details of Taguchi design method is as follows (Wu & Hamada, 2002):

- For each experiment, S/N ratio and its ANOVA table of mean quality attributes are calculated.
- For important factors, the factor with the highest S/N is selected.
- Each factor which does not have any important impact on S/N ratio and has significant impact on mean of the response will be selected in a way that is closer to the objective point.
- Factors which have important impact neither on S/N ratio nor on mean of response, are taken into consideration as economical factors.

Initial experiments show that different levels of considered parameters in Table 1 generate better results compared with other values. We use Taguchi method L16 to calibrate the parameters according to the levels and the number of the parameters shown in Table 1. In case we did not use this method, the number of necessary experiments for each instance would be $10 \times 4^3 = 640$.

Table 1

Algorithm parameters

Parameters	Levels
Crossover Rate (Rc)	0.7, 0.8, 0.9, 1.0
Mutation Rate (Rm)	0.025, 0.05, 0.1, 0.2
Population Size (popsize)	20, 30, 50, 100
Termination Criteria	100 iterations
Rep	20

For each instance, a relative percentage deviation (*RPD*) is defined as follows:

$$RPD = 100 \times \frac{S_{itr-\min_{i=1..d}}(S_i)}{\min_{i=1..d}(S_i)}$$

Itr, S_i and *d* denote index of trial, objective function value for trial *i* and total number of trials in the orthogonal array *L16*, respectively. 20 instances were considered for the adjustment of parameters. The main advantage of using *RPD* instead of objective function as response variable is the dimensionless property of these parameters which would not depend on the configuration of parts and machines. For each parameter, the related parameters are selected stochastically from the previous parameters. The *RPDs* for each instance are considered as a repeat for Taguchi method analysis. Tables 2 and 3 show the ANOVAs analysis related to *RPDs*. Also means of *RPD* and S/N ratio are depicted in Fig. 2 and Fig. 3. According to these tables and figures we can select the levels 0,025, 1.0 and 30 for mutation rate, crossover rate and population size, respectively.

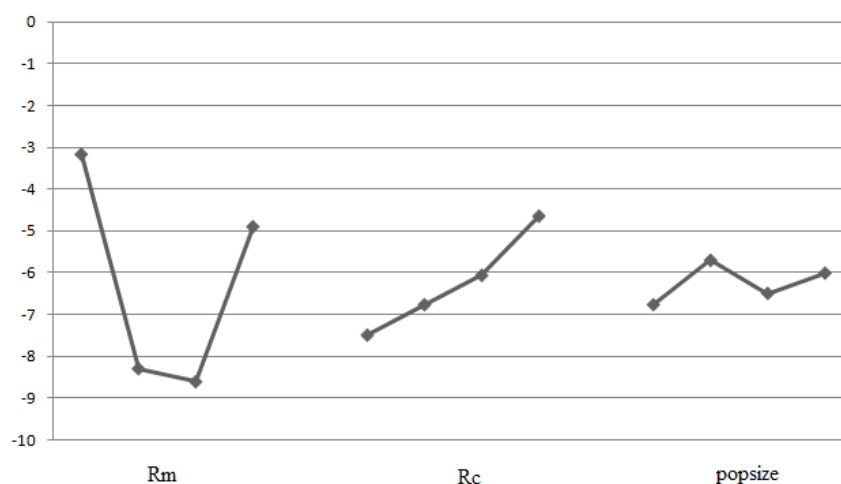


Fig. 2. The average S/N ratio plot at each level for RPD for algorithm calibration

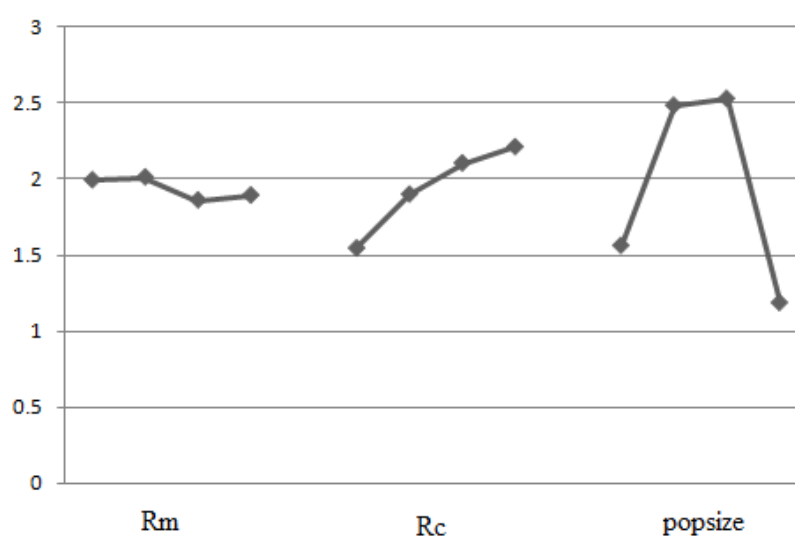


Fig. 3. Main effects plot for RPD values for algorithm calibration

Table 2

ANOVA input data for S/N ratios

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rm	3	2.74	2.74	0.9133	0.13	0.941
Rc	3	17.715	17.715	5.9049	0.82	0.528
Pop size	3	84.549	84.549	28.1829	3.92	0.073
Residual Error	6	43.129	43.129	7.1881		
Total	15	148.132				

Table 3

ANOVA RPD input data

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rm	3	0.06569	0.06569	0.0219	0.05	0.982
Rc	3	1.03122	1.03122	0.34374	0.83	0.522
Pop size	3	5.40573	5.40573	1.80191	4.37	0.059
Residual Error	6	2.4717	2.4717	0.41195		

4.2 Results

To evaluate the performance of the proposed model, eight different problems are considered shown in Table 4. Note that we consider the small-size problems since we compare the performance of GA algorithm and exact solution together. Since assembly details and scheduling aspects are not considered in the literature as the proposed models, the required data related are not available. Therefore, these input data are generated randomly. For each test problem, the model has been solved by LINGO 8.0 and compared with other two cases as follows:

- 1- For the first case, the model does not consider the scheduling. Therefore the objective function is to minimize the intercellular movements resulting due to processing and assembly operations.
- 2- For the second case, the model does not consider both the scheduling and the assembly details.

Table 4
The information of the eight benchmark problems

Problem #	Ref.	Problem specification				
		Number of non-assembly Items	Number of assembly items	Number of Operations	Number of Machines	Number of Cells
1	McCormick et al. (1972)	4	-	8	4	2
2	Xiaodan et al. (2007)	5	-	11	5	2
3	Heragu (1997)	6	-	15	7	2
4	Irani (1999)	6	-	14	10	3
5	Panchalavarapu and Chankong (2005)	7	7	15	8	2
6	Singh et al (1996)	8	-	23	6	2
7	Chan & Milner (1982)	10	-	46	15	3
8	McAuly (1972)	10	-	39	12	3

Table 5 summarizes the results of solutions and a comparison between the intercellular movements (IM) and cycle times (CT) for three situations. The computer machine used for solving is Pentium IV with CPU 2.GHz and RAM 1 GB.

Table 5
Computational experiments of intercellular movements (IM) and cycle time (CT) in three situations

Problem #	Proposed Model			Model without scheduling considerations			Model without scheduling and assembly considerations		
	IM due to processing	IM due to assembly	CT value	IM due to processing	IM due to assembly	CT value	IM due to processing	IM due to assembly	CT value
1	0	5	14216	0	0	16796	0	5	14216
2	51	4	7961	0	0	10009410	0	0	10584
3	2090	15	21855	0	9	10003100	0	11	30163
4	455	10	11504	130	4	17585	130	12	17596
5	0	5	300	1	1	320	1	11	10000260
6	2014	8	16709	1590	8	28193	1590	19	28221
7	4732	23	31623	0	20	54859	0	29	54253
8	1596	15	35376	1246	15	62966	1246	19	10001260

In addition, using the proposed GA, the solutions are obtained and they are compared with corresponding solution of LINGO. The deviation of GA solution from the optimum value is calculated to compare the performance of the proposed GA with optimal solutions.

$$Deviation = \frac{CT^{GA} - CT^*}{CT^*}$$

Table 6

Computational results of the proposed method using direct implementation and GA

Problem # (i)	Optimum solution of LINGO		Best solution of GA		Deviation (D_i) %
	CT^* value	CPU Time	CT value	CPU Time	
1	14216	00:00:01	14216	00:00:02	0.00%
2	7961	00:00:00	8017	00:00:03	0.70%
3	21855	00:00:01	23122	00:00:04	5.80%
4	11504	00:00:01	12896	00:00:03	12.10%
5	300	00:00:03	320	00:00:04	6.67%
6	16709	00:00:05	16709	00:00:04	0.00%
7	31623	00:01:58	32362	00:00:07	2.34%
8	35376	00:00:18	37054	00:00:07	4.74%

Based on results of Table 5, we can see that the CT^* values of the integrated model are lower than the time the model do not consider the scheduling parameters. Also, it is clear that the number of intercellular movements (IM) resulting due to assembly for model without assembly consideration is higher than the time this aspect is integrated with the CMS design problem. Table 6 also shows the details of the performance of the proposed model in terms of the CPU times and the objective function. As we can observe, there are two cases where both methods find the same optimal results and in other cases, the near-optimal solutions achieved by GA are fairly close to the optimal solutions.

5. Conclusion

In this paper, we have presented a new mathematical model for CMS design problem included cell formation and scheduling simultaneously where also the assembly operations and product structure are taken into consideration. The proposed model was formulated as nonlinear mixed integer programming and then has been simplified using some auxiliary binary variables. The resulted model was solved for some small problems and a GA method has been introduced to solve the proposed model for large-scale problems. The results of the proposed GA were compared with optimal solutions for some different problems in the literature. As a possible future research, one could consider the model with two objective functions including minimizing intercellular movements and minimizing cycle time of finished product.

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